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## Worksheet \#15: Justifications Practice



This is the graph of $f^{\prime}(x)$, the derivative of $f(x) \cdot f^{\prime}(x)$ has horizontal tangents when $\mathrm{x}=3$, $\mathrm{x}=0$, and $\mathrm{x}=-3$. Justify each of the following responses.
A) For what value(s) of $x$ does $f$ have a relative maximum?
B) For what value(s) of $x$ does $f$ have a relative minimum?
C) For what interval(s) of $x$ is $f$ concave downwards?
D) For what interval(s) of $x$ is $f$ decreasing?
E) At $x=3$, $\operatorname{does} f$ have a relative min, relative max, or point of inflection? Explain.
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This is the graph of $h$ on the interval $[-6,5]$. Let $g(x)=\int_{0}^{x} h(t) d t$.
A) For what value(s) of $x$ on the open interval $(-6,5)$ is $h^{\prime}$ undefined? Explain.
B) Find $h^{\prime}(-3)$ and $h^{\prime}(0)$.
C) Find $g(2)$.
D) For what value(s) of $x$, if any, does $g$ have a relative maximum? Justify.
E) For what value(s) of $x$, if any, does $g$ have a relative minimum? Justify.
F) For what value(s) of $x$ on the open interval ( $-6,5$ ), if any, does $g$ have a point of inflection? Justify.
G) For what interval(s) of $x$ on the open interval $(-6,5)$ is $g$ concave upwards? Justify.

