$$
f(t)= \begin{cases}g(t) & \text { for } 0 \leq t \leq 12 \\ \frac{t^{2}}{8}-3 t+83 & \text { for } 12<t \leq 24\end{cases}
$$

| $t$ (hours) | 0 | 4 | 6 | 8 | 12 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $g(t)$ (degrees Fahrenheit) | 87 | 81.5 | 76 | 70.5 | 65 |

The temperature of a room, in degrees Fahrenheit, on a certain day is modeled by the function $f$ defined above, where $g$ is a continuous function and $t$ is measured in hours. Values of $g(t)$ at selected values of $t$ are given in the table above.
(a) According to the model $f$, what is the average rate of change of the temperature of the room over the time interval $0 \leq t \leq 12$ hours? Include units on your answer.
(b) Use the data in the table to approximate $f^{\prime}(10)$. Show the computations that lead to your answer.
(c) Is $f$ continuous when $t=12$ ? Justify your answer.
(d) Find the exact value of $f^{\prime}(20)$. Interpret the meaning of this value in the context of the problem.

