## What are some things we already know about right triangles?

## Trigonometric Functions

| WORDS | NUMBERS | SYMBOLS |
| :---: | :---: | :---: |
| The sine $(\sin )$ of angle $\theta$ is the ratio of the length of the opposite leg to the length of the hypotenuse. | $\sin \theta=\frac{4}{5}$$\cos \theta=\frac{3}{5}$ | $\sin \theta=\frac{\text { opp. }}{\text { hyp. }}$ |
| The cosine (cos) of angle $\theta$ is the ratio of the length of the adjacent leg to the length of the hypotenuse. |  | $\cos \theta=\frac{\text { adj }}{\text { hyp. }}$ |
| The tangent (tan) of angle $\theta$ is the ratio of the length of the opposite leg to the length of the adjacent leg. |  | $\tan \theta=\frac{\text { opp. }}{\text { adj. }}$ |

Example \#1:
Find the value of the sine, cosine, and tangent functions for $\boldsymbol{\theta}$.


## Example \#2:

A skateboard ramp will have a height of 12 in., and the angle between the ramp and the ground will be $17^{\circ}$. To the nearest inch, what will be the length $l$ of the ramp?

You try: A school is constructing a wheelchair ramp from the ground to a deck with a height of 18in. The angle between the ground and the ramp must be $4.8^{\circ}$. To the nearest inch, what should be the distance $d$ between the end of the ramp and the deck?

## Special Right Triangle Trig Ratios:

45-45-90

30-60-90

## Example \#3: Use a trig function to find the value of $\boldsymbol{x}$ without a

 calculator.

## You try: Now find the other side length of the triangle.

## Reciprocal Trigonometric Functions

| WORDS | NUMBERS | SYMBOLS |
| :--- | :--- | :--- |
| The $\operatorname{cosecant~(csc)~of~angle~} \theta$ <br> is the reciprocal of the $\operatorname{sine}$ <br> function. | $\csc \theta=\frac{5}{4}$ | $\csc \theta=\frac{1}{\sin \theta}=\frac{\text { hyp. }}{\text { opp. }}$ |
| The secant (sec) of angle $\theta$ <br> is the reciprocal of the $\operatorname{cosine}$ <br> function. | $\sec \theta=\frac{5}{3}$ | $\cos$ |
| The cotangent (cot) of <br> angle $\theta$ is the reciprocal of <br> the tangent function. | $\cot \theta=\frac{3}{4}$ | $\sec \theta=\frac{1}{\cos \theta}=\frac{\text { hyp. }}{\text { adj. }}$ |

Example \#4: Find the values of the six trigonometric functions for $\boldsymbol{\theta}$.

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## You try:

1. A boy flying a kite lets out 300 feet of string that makes an angle of $38^{\circ}$ with the ground. Assuming that the string is straight, how high above the ground is the kite?
2. A decorative pin is in the shape of an equilateral triangle. The length of each side is 6 centimeters. Josh will attach the fastener to the back along the height of the pin. Will the fastener fit if it is 4 centimeters long?
3. A straight road to the top of a hill is 2500 feet long and makes an angle of $12^{\circ}$ with the horizontal. Find the height of the hill.
4. A manufacturer wants to make an equilateral case with a height of 30 centimeters. What is the length of each side of the case? Round to the nearest tenth.

Write about it: Suppose you are given the measure of an acute angle in a right triangle and the length of the leg adjacent to this angle. Describe $\mathbf{2}$ different methods that you could use to find the length of the hypotenuse.

